



**SIGGRAPH 2023**  
**LOS ANGELES+ 6-10 AUG**

THE PREMIER CONFERENCE & EXHIBITION ON  
COMPUTER GRAPHICS & INTERACTIVE TECHNIQUES

# DIFFERENTIABLE HEIGHTFIELD PATH TRACING WITH ACCELERATED DISCONTINUITIES

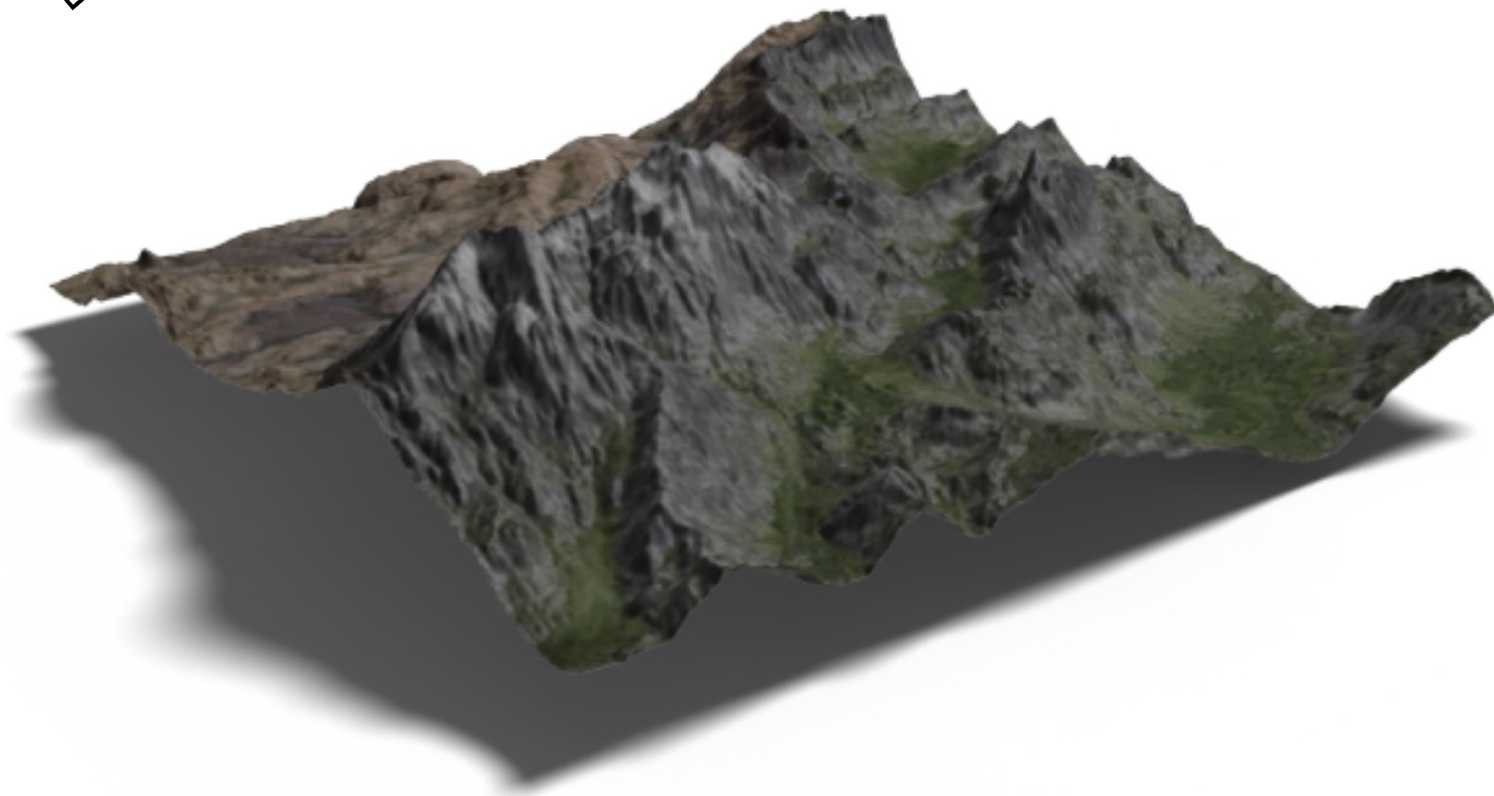
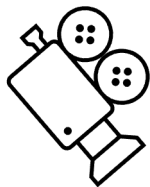
**XIAOCHUN TONG**, UNIVERSITY OF WATERLOO

**HSUEH-TI DEREK LIU**, ROBLOX

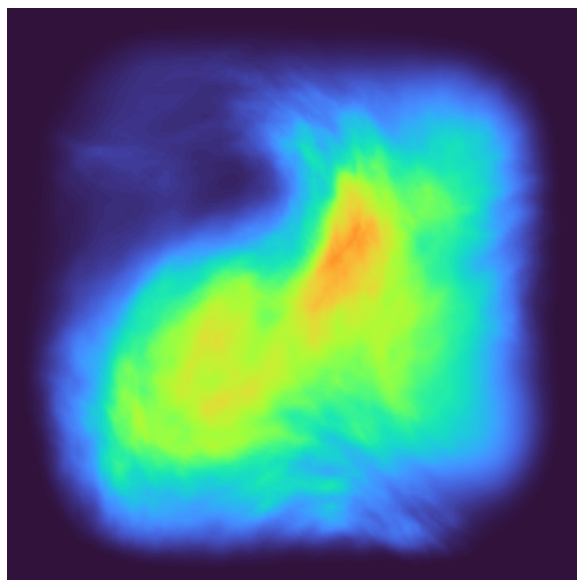
**YOTAM GINGOLD**, GEORGE MASON UNIVERSITY

**ALEC JACOBSON**, UNIVERSITY OF TORONTO & ADOBE RESEARCH

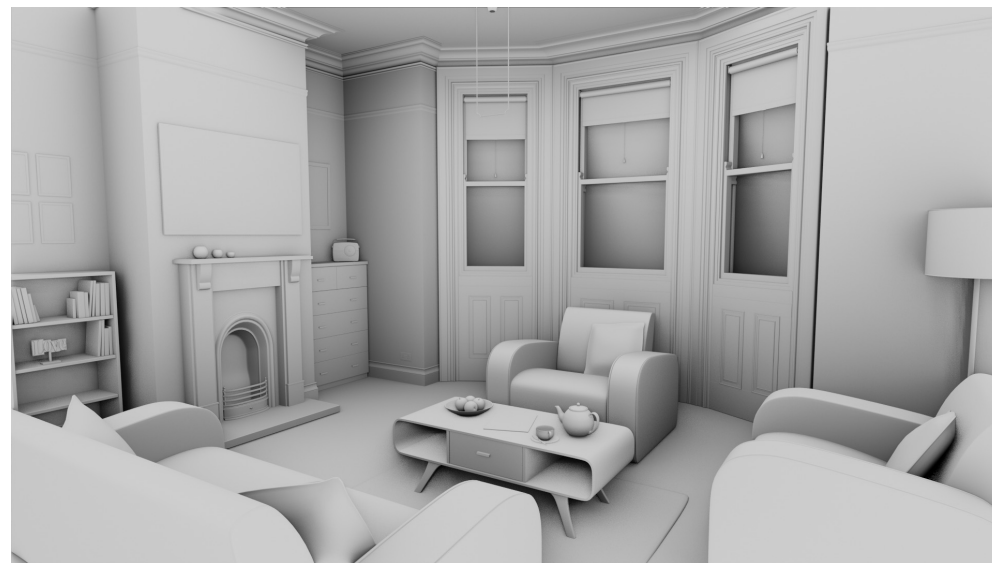
# → FAST DIFFERENTIABLE HEIGHTFIELD RENDERER



- Geometry representation using 2D scalar fields



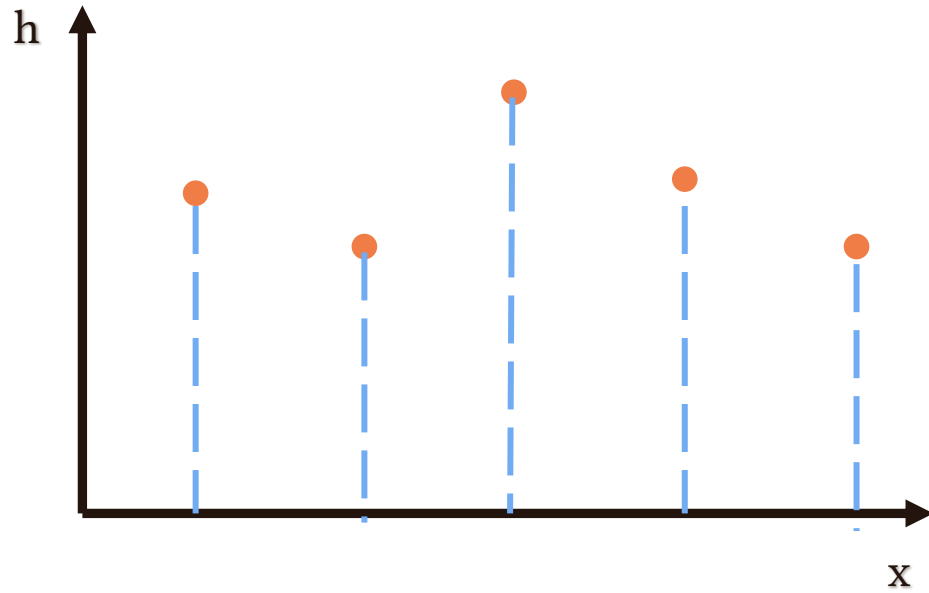
Terrain



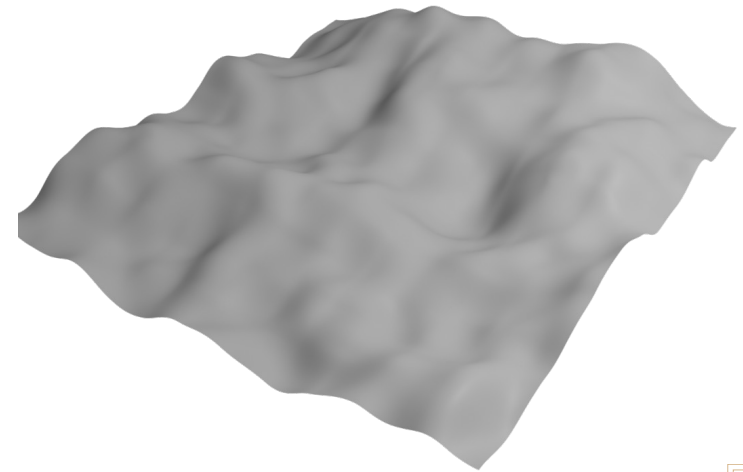
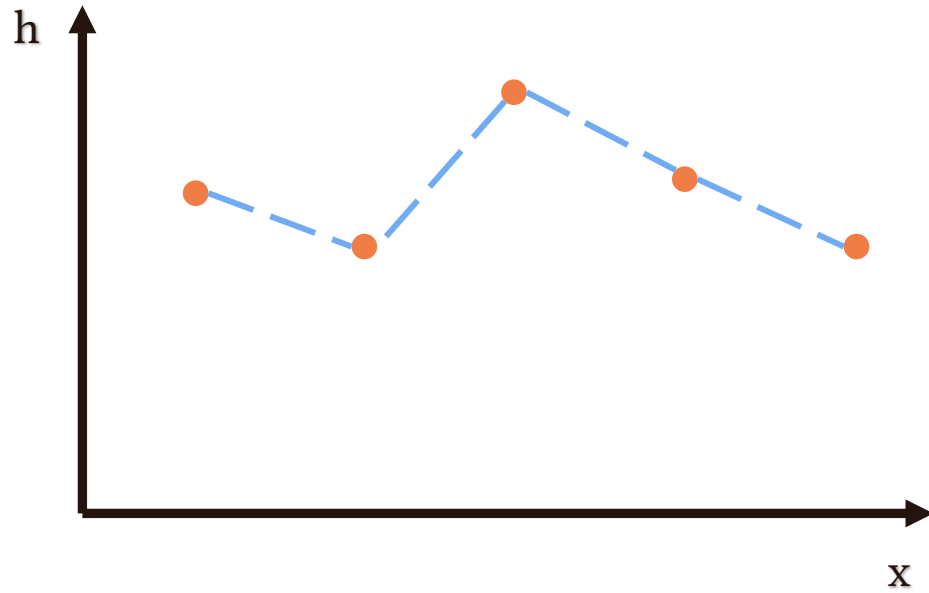
Screen space rendering



# → DISCONTINUITIES ON HEIGHTFIELD



# → DISCONTINUITIES ON HEIGHTFIELD

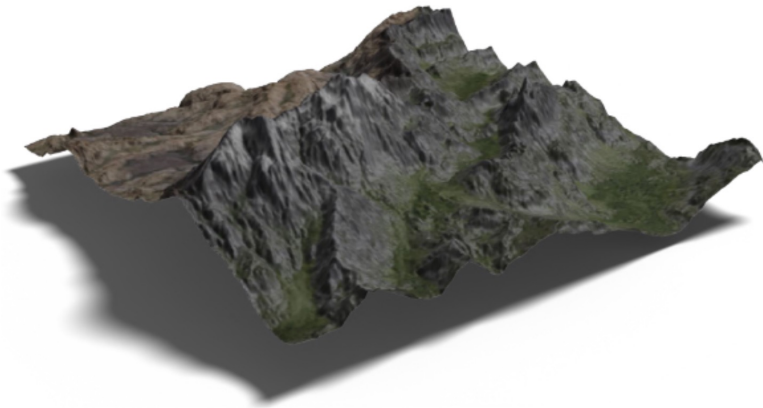
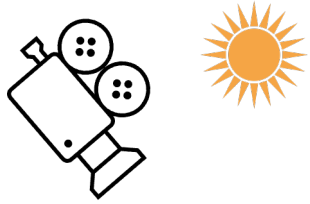




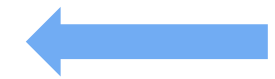
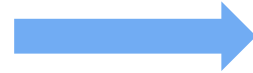
# DIFFERENTIABLE HEIGHTFIELD PATH TRACING



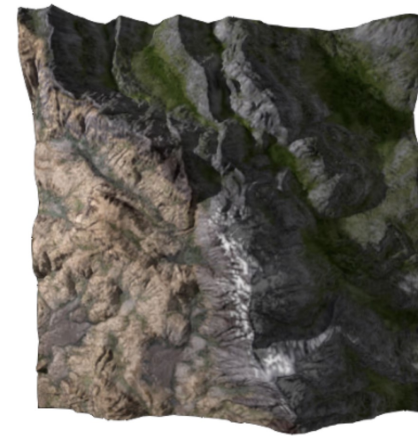
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Forward pass



Backward pass



optimized rendering



target image



# → DIFFERENTIABLE HEIGHTFIELD PATH TRACING

- Light transport equation

$$L_o(\mathbf{x}, \omega_o, h) = L_e(\mathbf{x}, h) + \int_{\Omega} L_i(\mathbf{x}, \omega_i, h) f(\mathbf{x}, \omega_o, \omega_i, h) d\omega_i^{\perp}$$

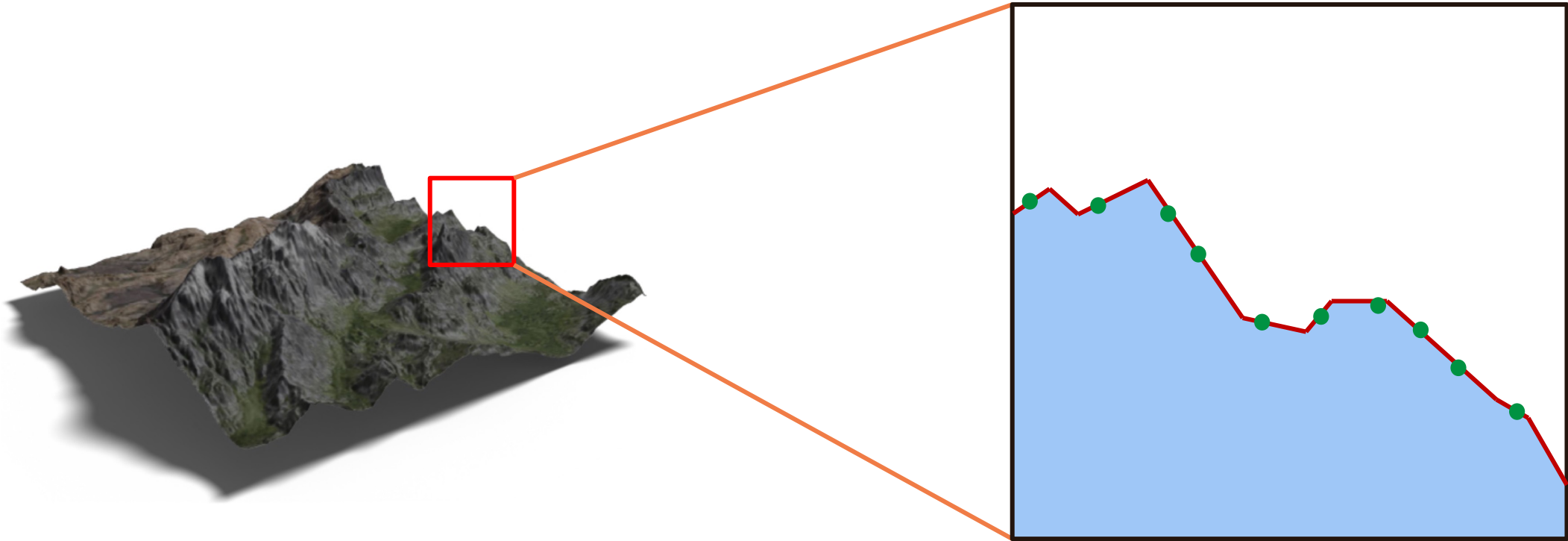
- Differentiating continuous integrand is can be done efficiently [Nimier-David et al. 2020; Zeltner et al. 2021]

$$\begin{aligned} \frac{\partial L_o(\mathbf{x}, \omega_o, h)}{\partial h} &= \frac{\partial}{\partial h} \int_{\Omega} L_i(\mathbf{x}, \omega_i, h) f(\mathbf{x}, \omega_o, \omega_i, h) d\omega_i^{\perp} \\ &= \int_{\Omega} \frac{\partial}{\partial h} L_i(\mathbf{x}, \omega_i, h) f(\mathbf{x}, \omega_o, \omega_i, h) d\omega_i^{\perp} \\ &\quad + \int_{\Omega} \frac{\partial L_i(\mathbf{x}, \omega_i, h)}{\partial h} f(\mathbf{x}, \omega_o, \omega_i, h) d\omega_i^{\perp} \end{aligned}$$

Bottleneck is differentiating discontinuities!



# → DISCONTINUITIES ON HEIGHTFIELD

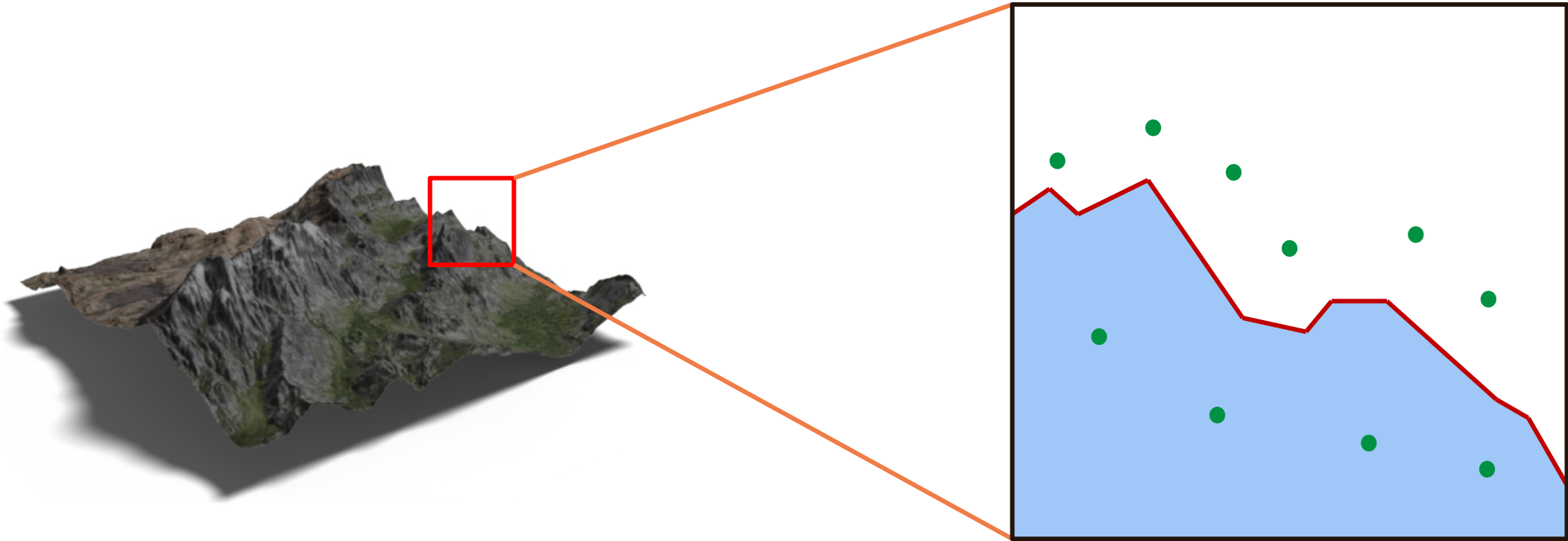


[Li et al . 2018]





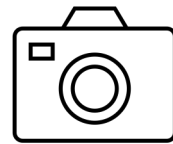
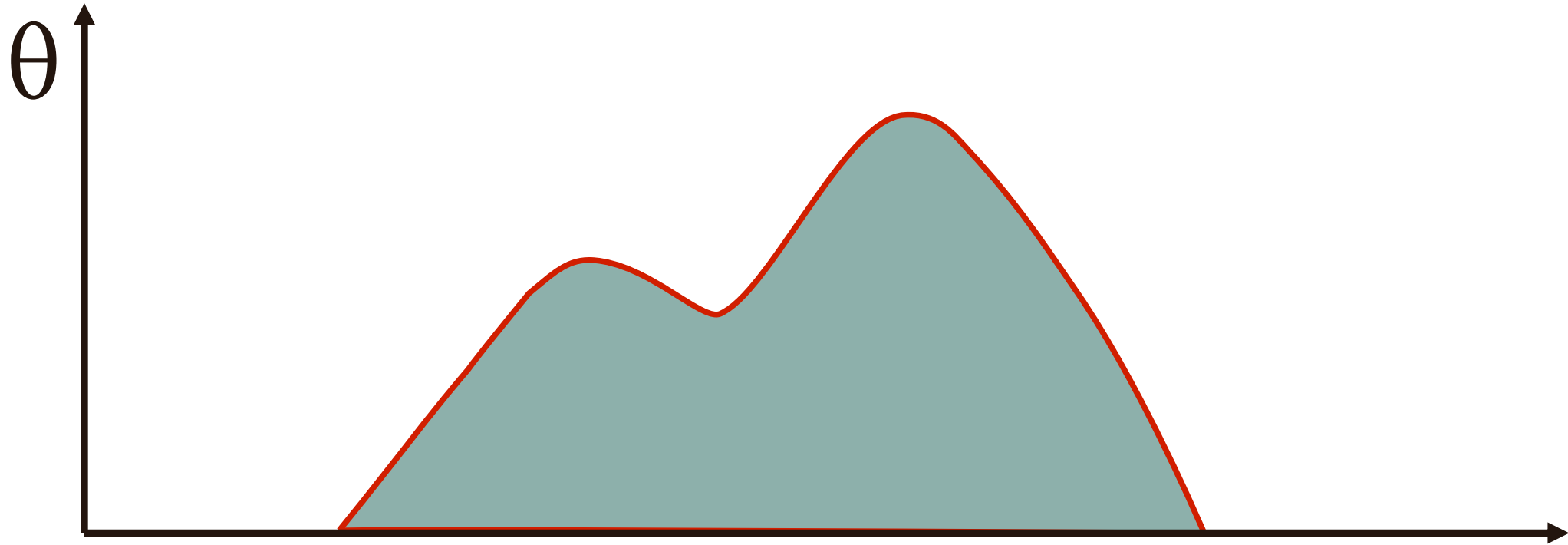
# → DISCONTINUITIES ON HEIGHTFIELD



[Loubet et al. 2019]



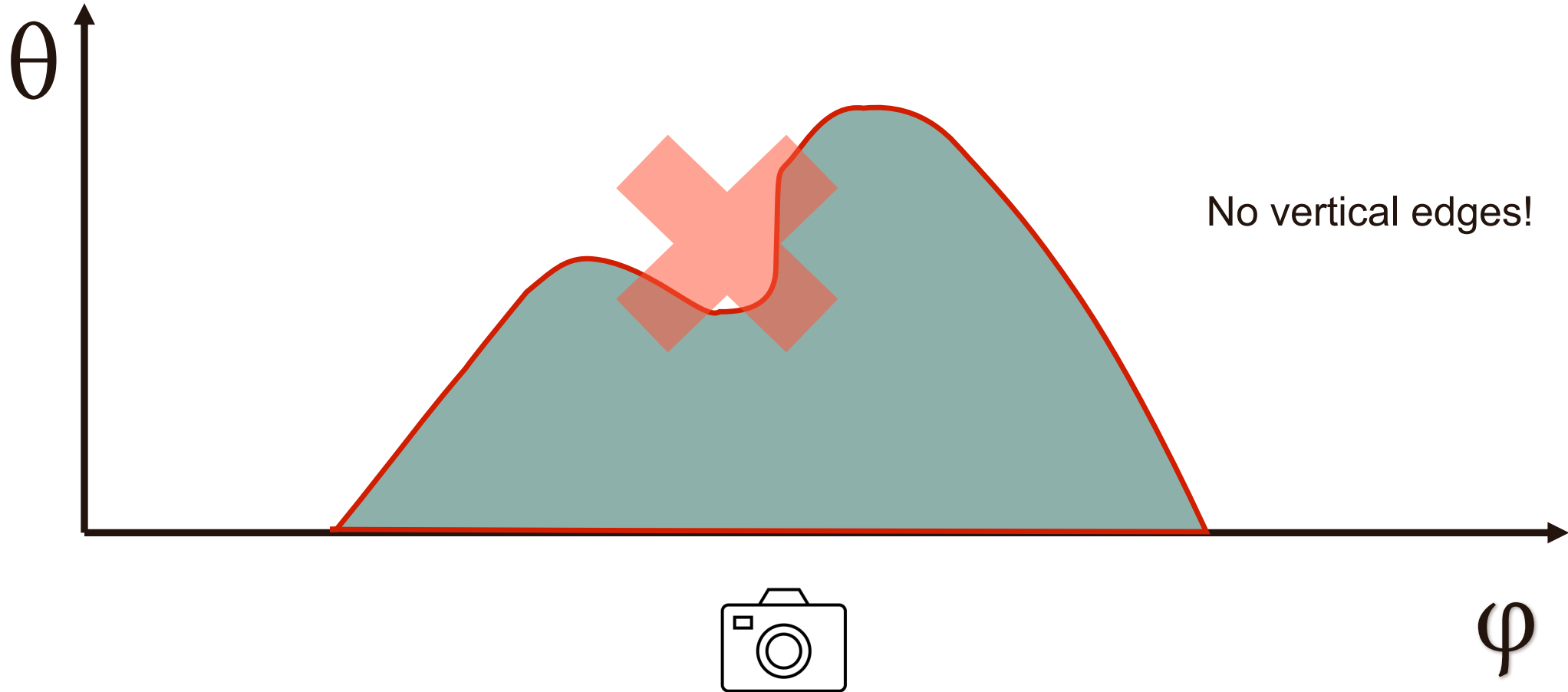
# → DISCONTINUITIES ON HEIGHTFIELD



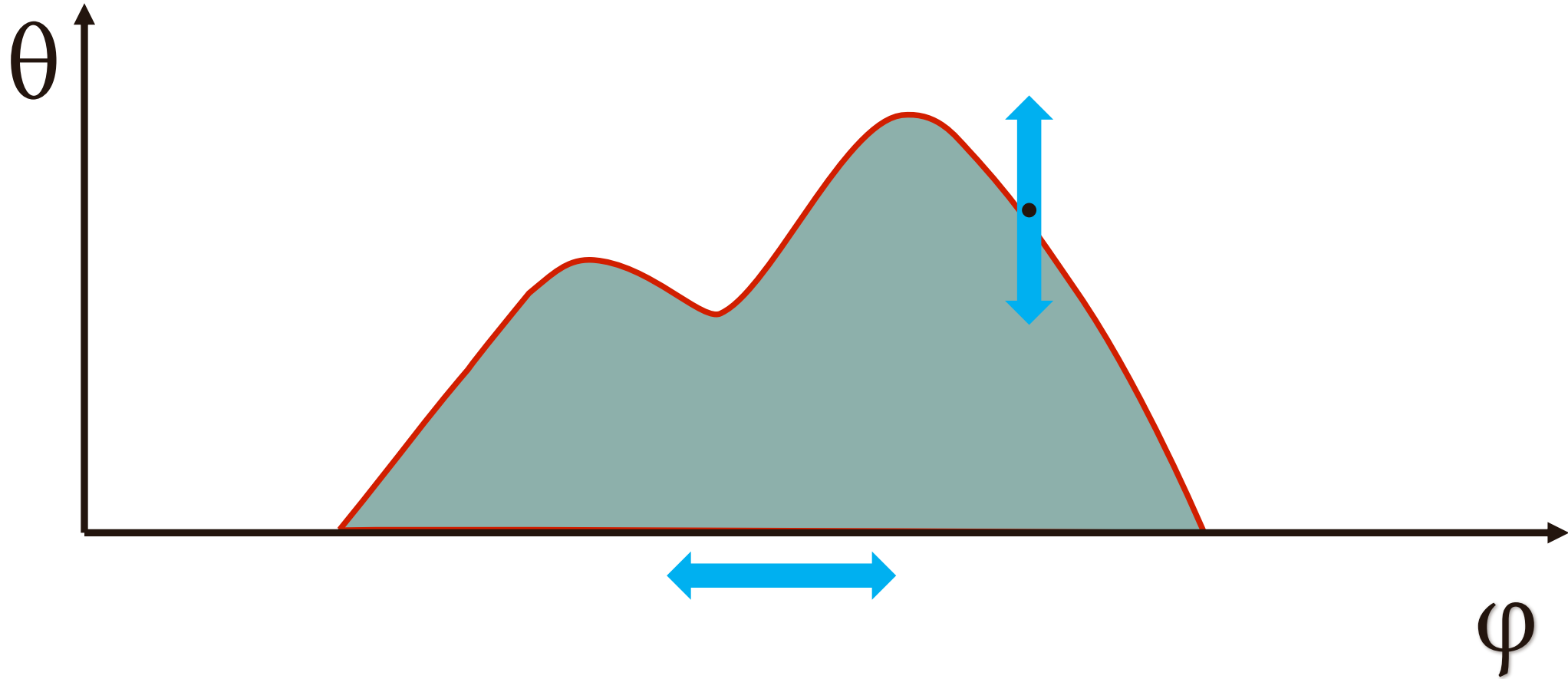
$\varphi$



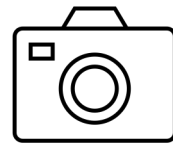
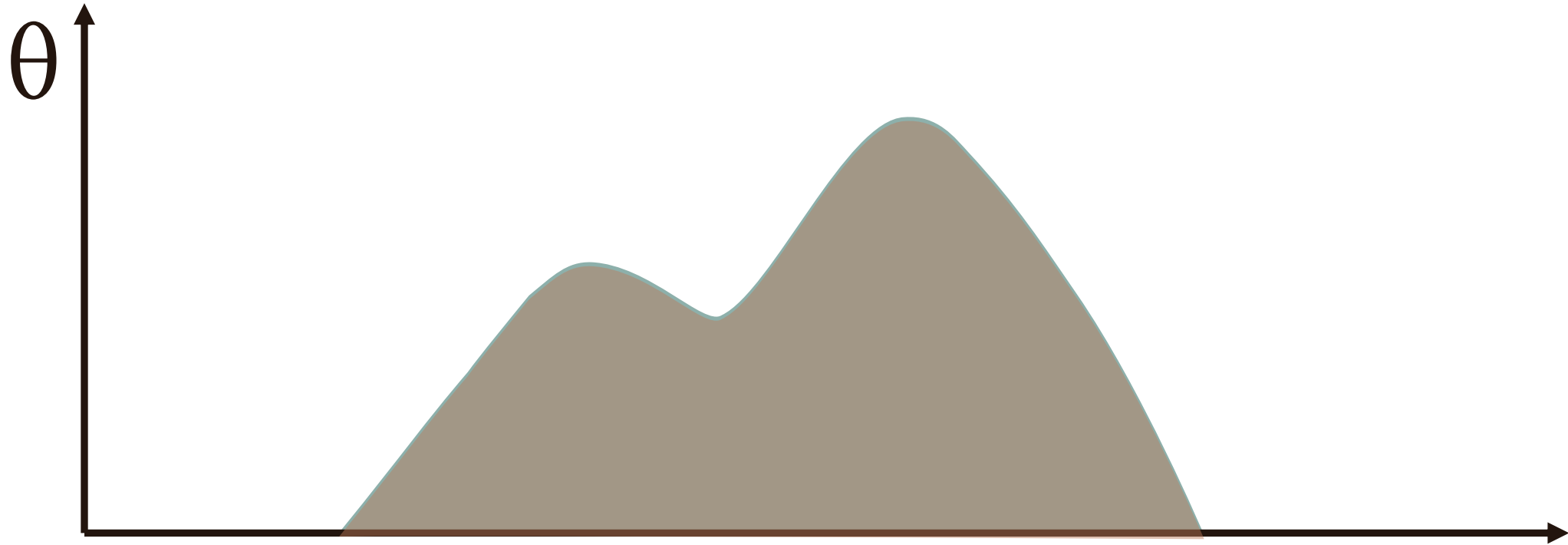
# → DISCONTINUITIES ON HEIGHTFIELD



# → DISCONTINUITIES ON HEIGHTFIELD



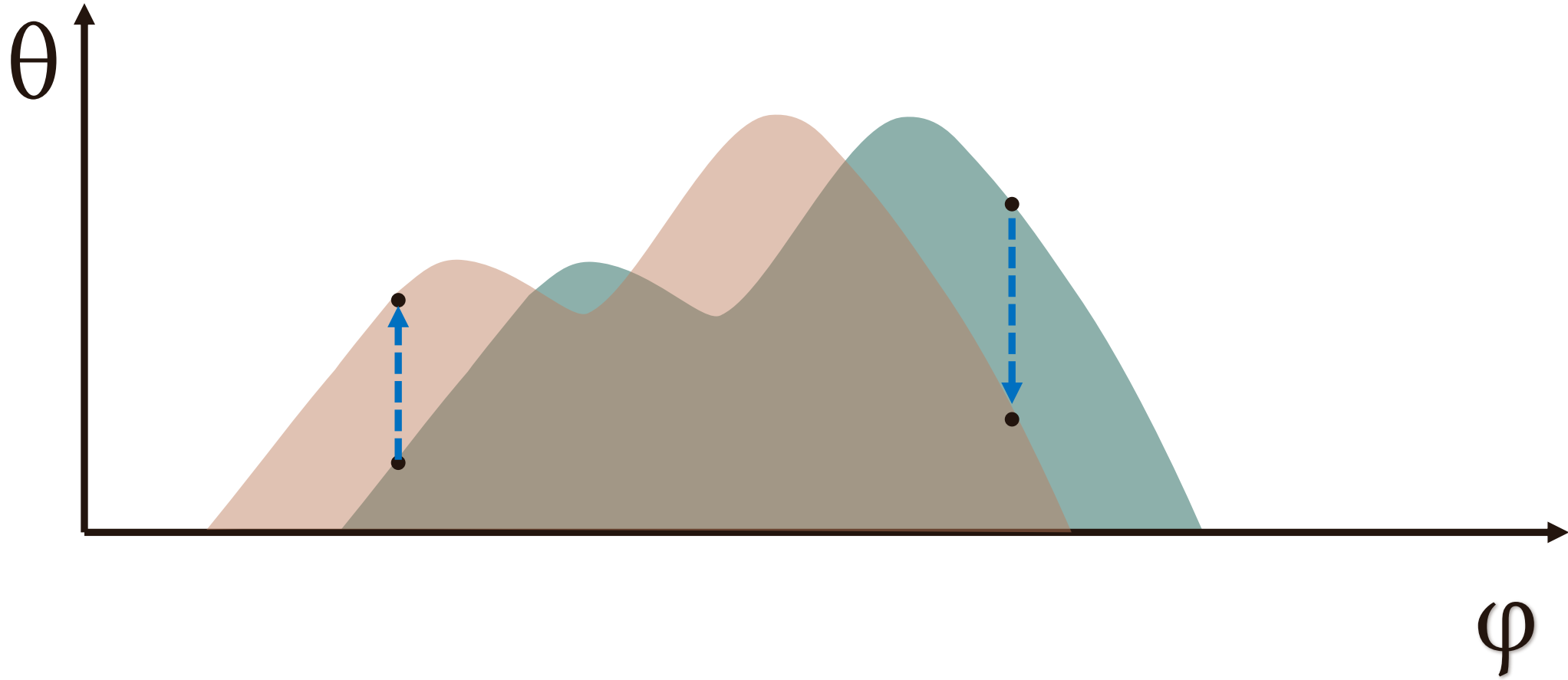
# → DISCONTINUITIES ON HEIGHTFIELD



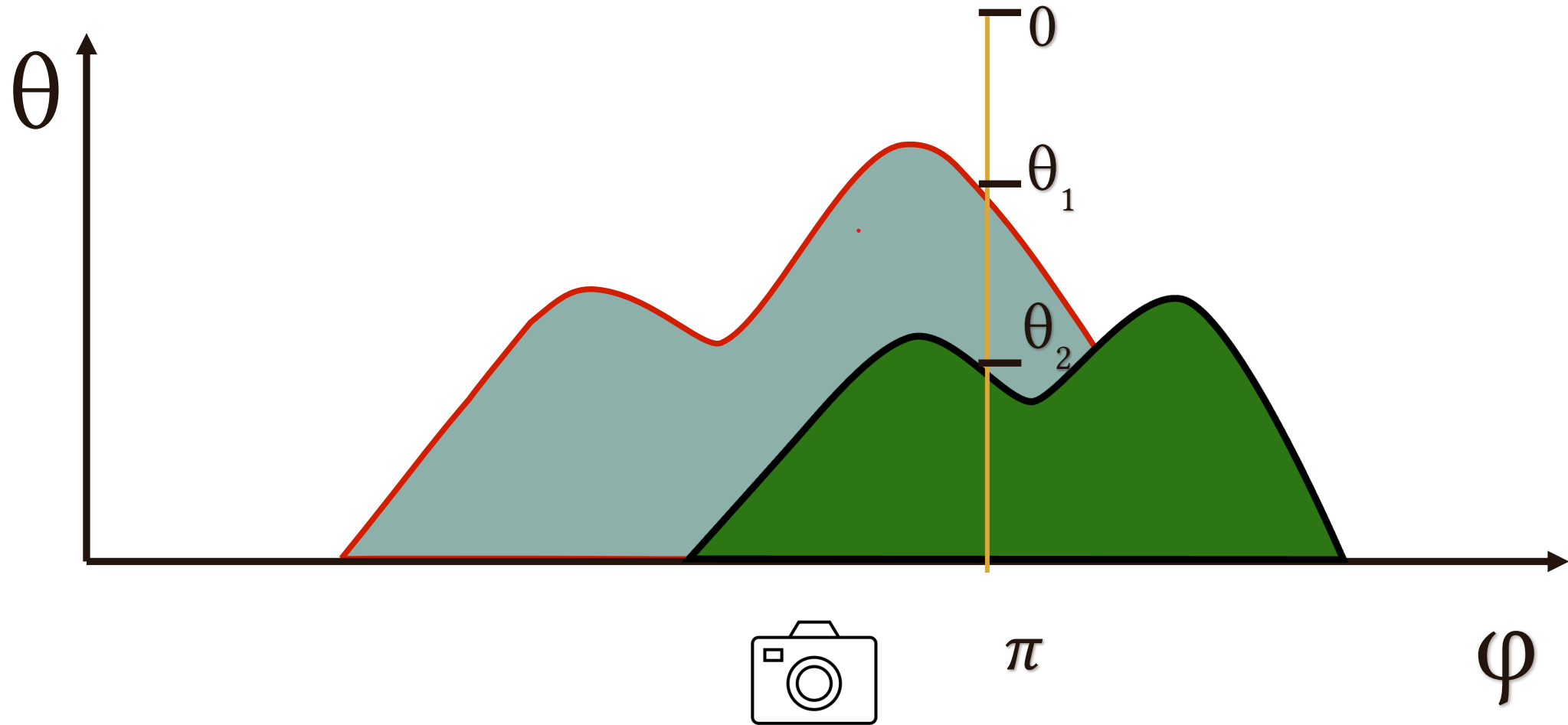
$\varphi$



# → DISCONTINUITIES ON HEIGHTFIELD



# → DISCONTINUITIES ON HEIGHTFIELD



# → REPARAMETERIZE DISCONTINUITIES

## ➤ Reparameterization

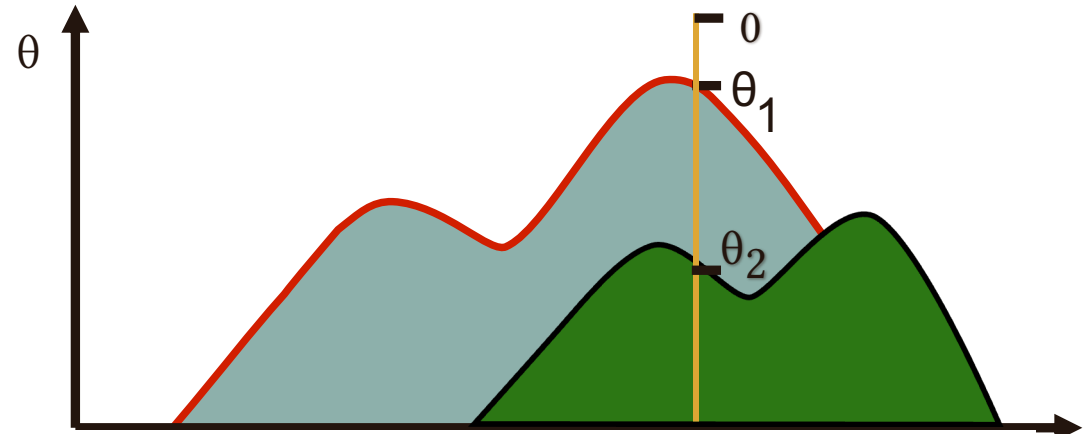
- Make the integral bound independent of scene parameters  $h$

$$I = \int_0^\pi f(\theta) d\theta$$

$$I = \int_0^{\theta_1} f_1 d\theta + \int_{\theta_1}^{\theta_2} f_2 d\theta + \int_{\theta_1}^\pi f_3 d\theta$$

$$T_i(u) = (1 - u)\theta_i + u\theta_{i+1}$$

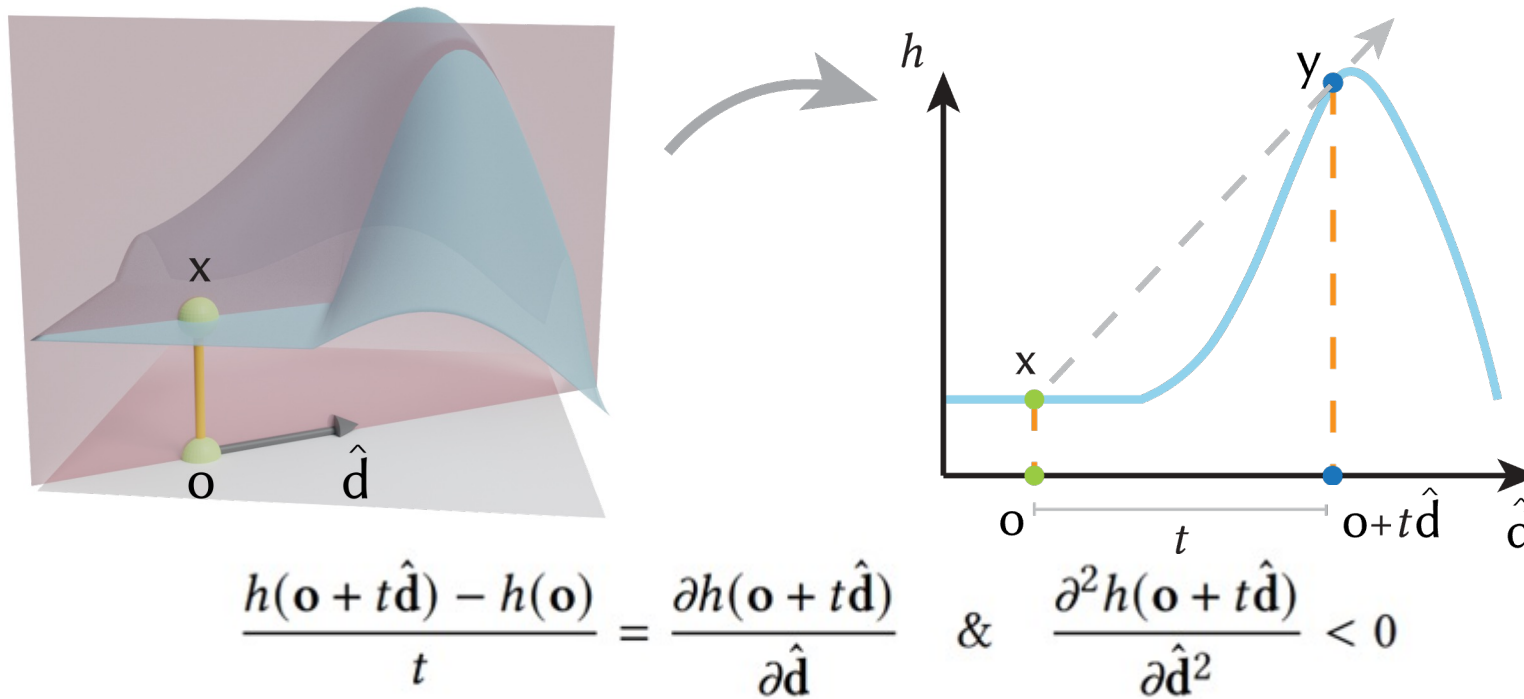
$$I = \int_0^1 f_1 \underline{T_1} du + \int_0^1 f_2 \underline{T_2} du + \int_0^1 f_3 \underline{T_3} du$$





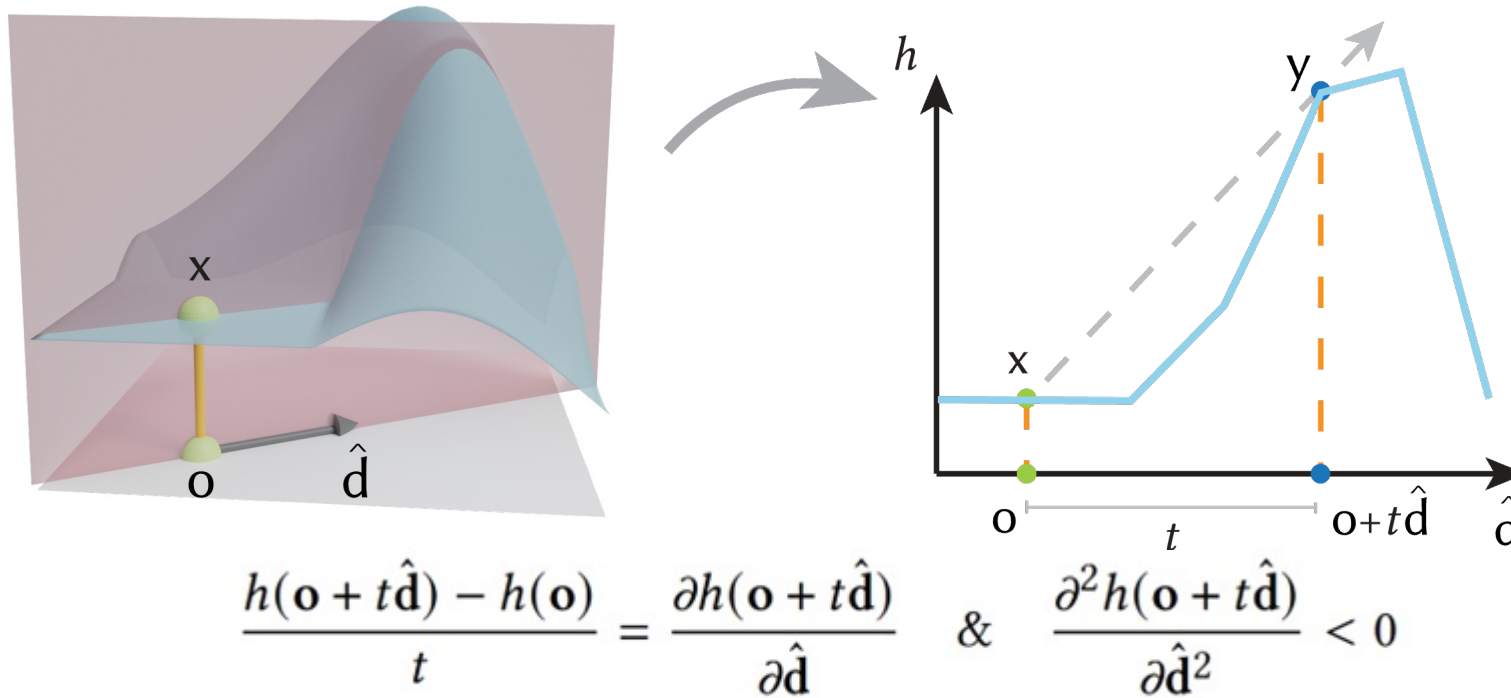
# → DETERMINING DISCONTINUITIES

➤ Discontinuities are points where ray is tangent to the surface



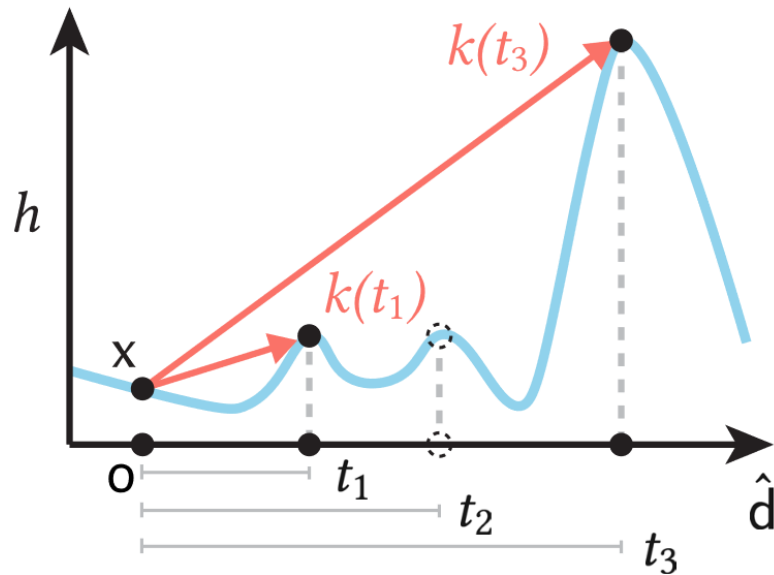
# → DETERMINING DISCONTINUITIES

➤ Discontinuities are points where ray is tangent to the surface



# → ACCELERATE DISCONTINUITY SEARCHING

- Lower, further discontinuities are blocked by near higher discontinuities
- Optimization: track *the current minimum slope* during mipmap ray tracing

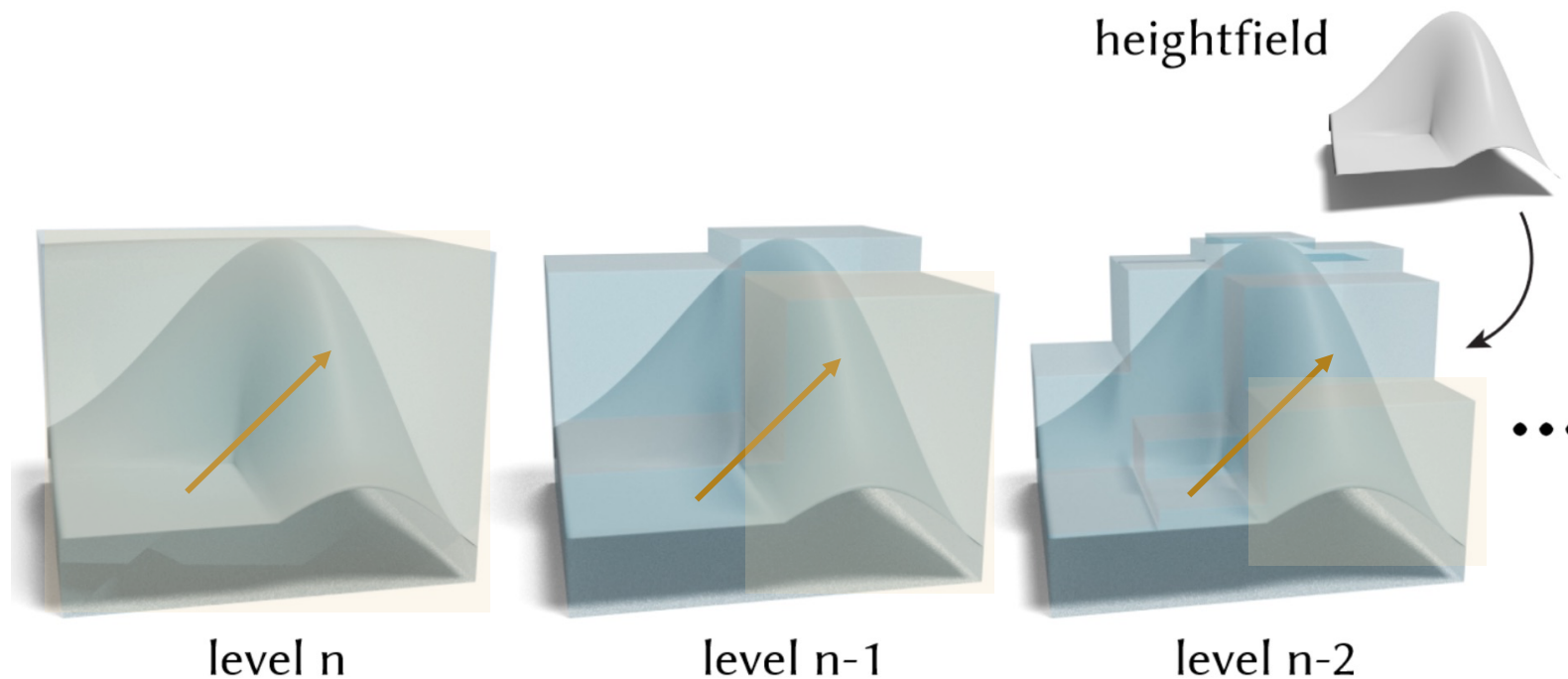


$$k(t) = \frac{h(\mathbf{o} + t\hat{\mathbf{d}}) - h(\mathbf{o})}{t}$$

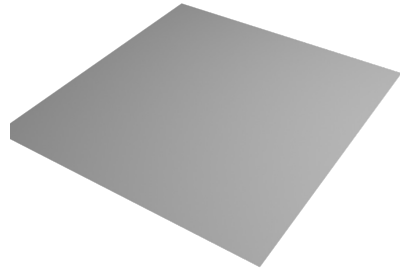


# → HEIGHTFIELD (BACKWARD) RENDERING [TODO]

- Skip regions *below* the ray with *current minimum slope*
  - Accelerate with maximum mipmap [Tevset al. 2008]!



# → DIFFERENTIABLE HEIGHTFIELD PATH TRACING

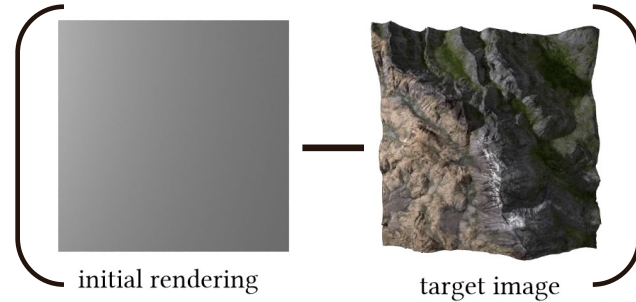


initial height field

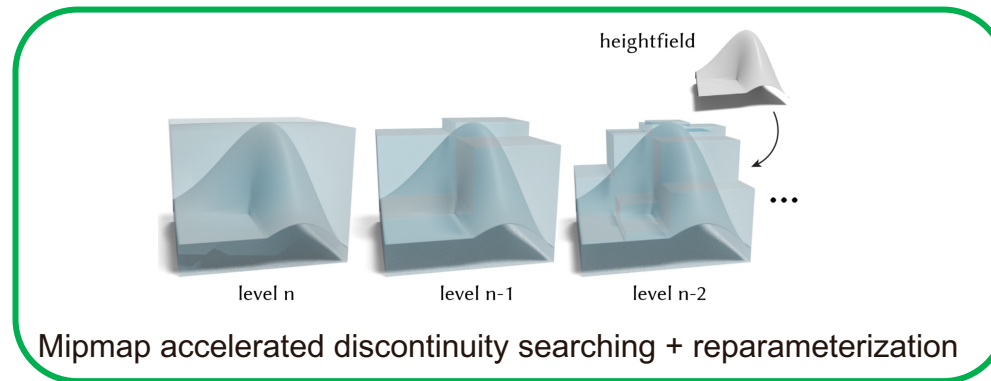
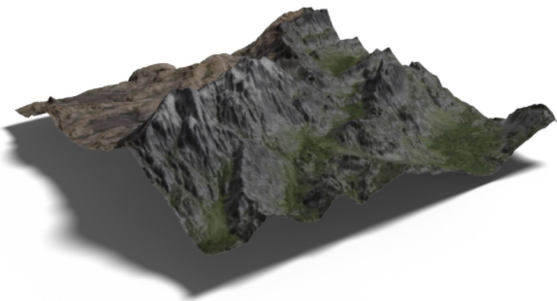


Forward rendering

Loss

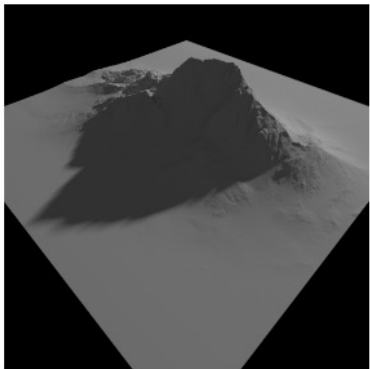


— Forward pass  
— Backward pass

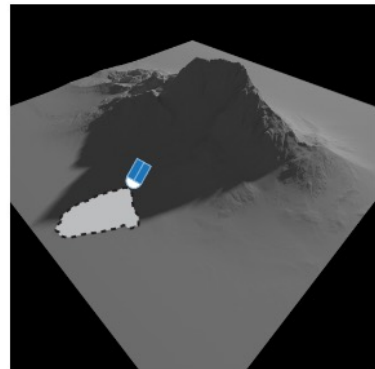


# → REALTIME SHADOW EDITING

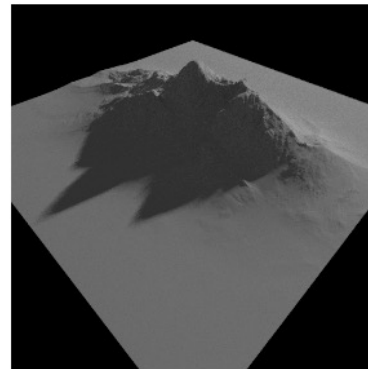
- > 300 spp/s



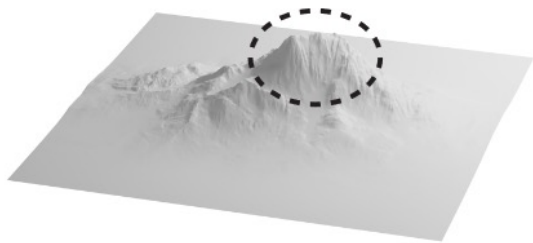
initial rendering



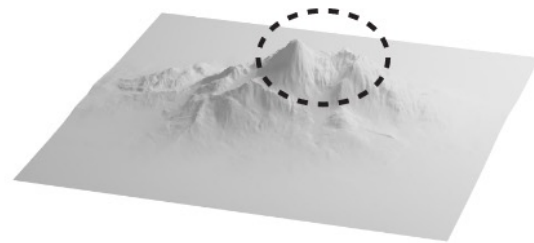
user erases shadow



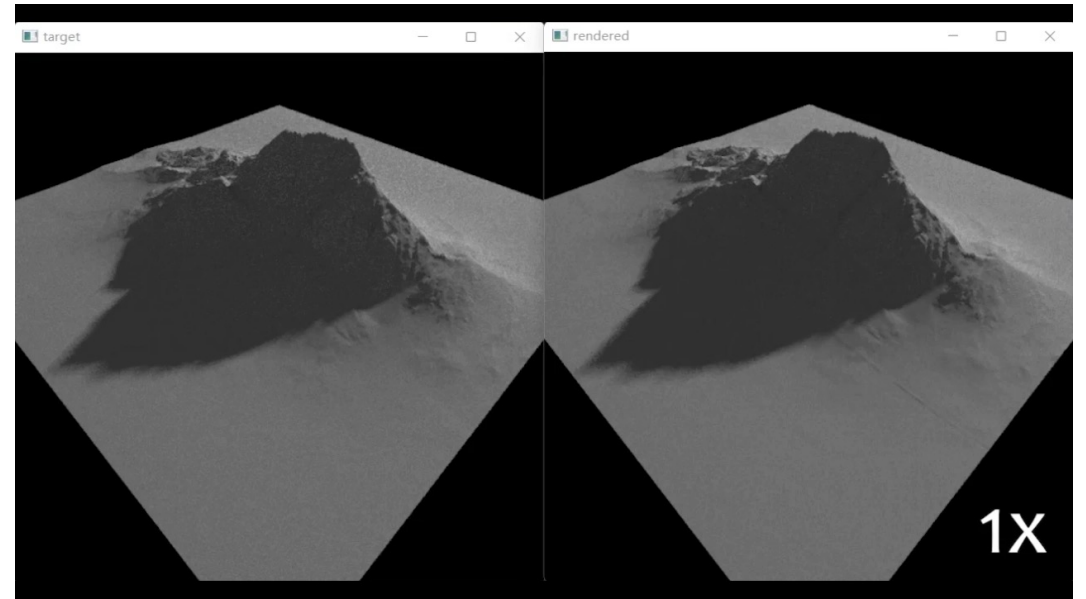
optimized rendering



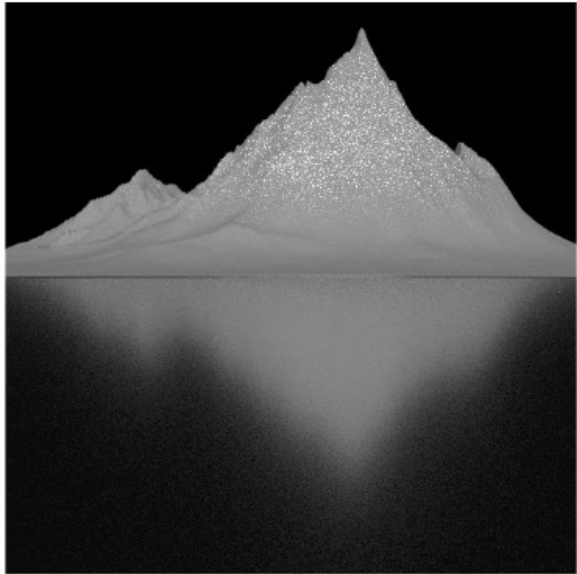
initial geometry



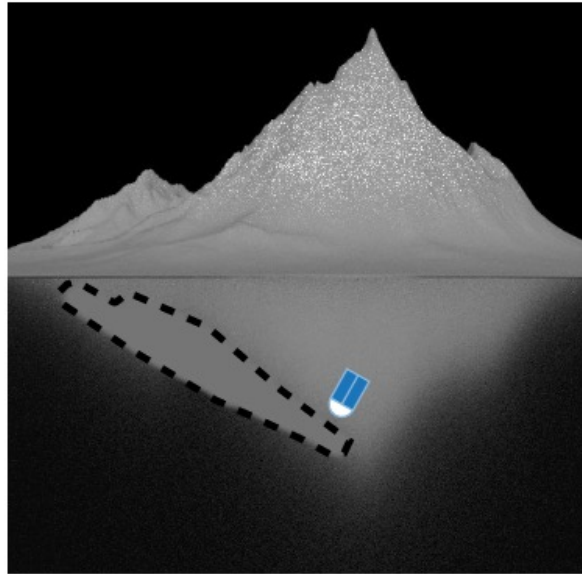
optimized geometry



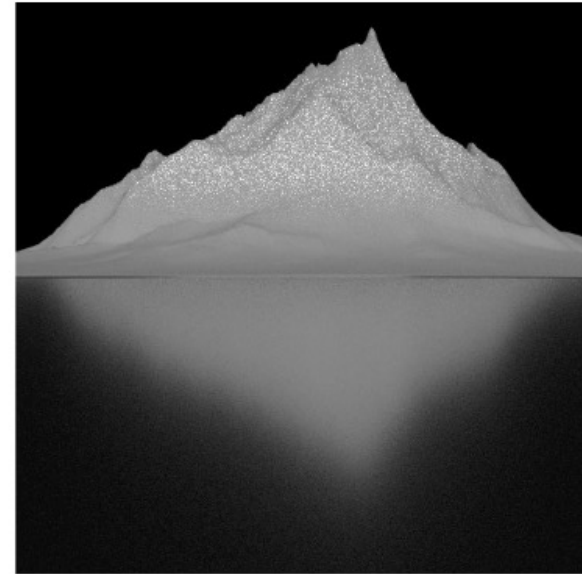
# → GLOSSY REFLECTION EDITING



initial rendering



user edits reflection



optimized rendering





# INVERSE RENDERING



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## ➤ Multiview surface reconstruction with global illumination



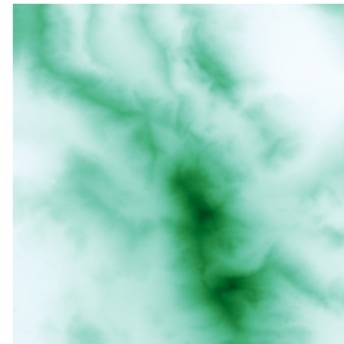
initial rendering



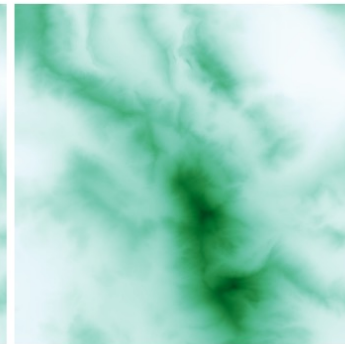
optimized rendering



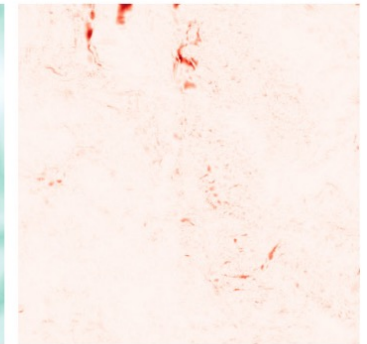
target image



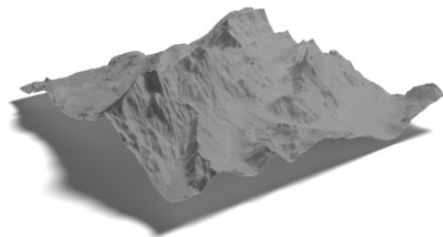
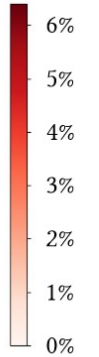
optimized height



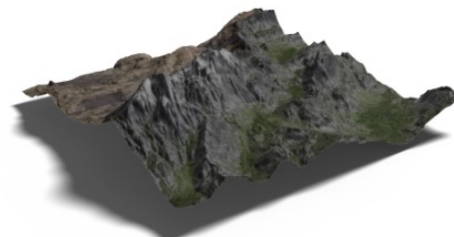
target height



error



optimized height field



with optimized texture



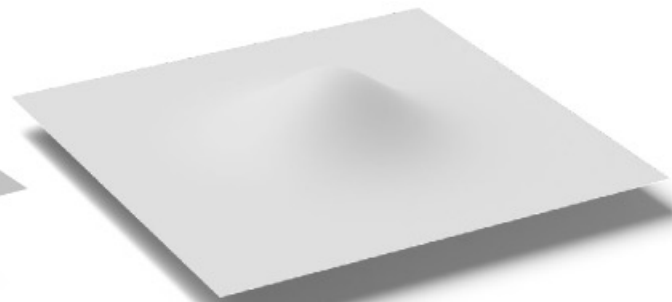
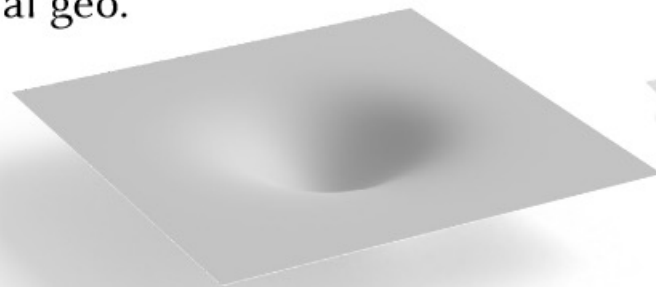


- Generate heightfield & material from text prompt using CLIP [Radford et al. 2021]

**“crater on the moon”**

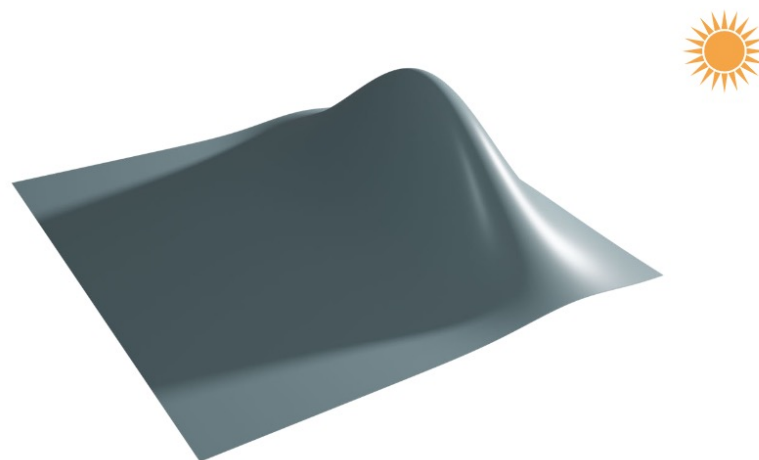
**“volcano and a river of lava”**

initial geo.



## → FUTURE WORK

- Improving convergence rate for glossy material
- Improving performance where scene has few discontinuities
- Explore more interactive applications with differentiable renderers



- Smooth heightfield with few discontinuities



# → ACKNOWLEDGEMENT



## THANK YOU!

Xiaochun Tong

[xtong@uwaterloo.ca](mailto:xtong@uwaterloo.ca)

